Investigation of multiple cracking in glass/epoxy 2D woven composites by vibrothermography

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Abstract

An experimental study about the application of vibrothermography for the investigation of multiple micro-cracking in woven composites is here reported. The material is first damaged during tensile loading tests in order to have samples that present increasingly damaged states. The goal of the study is to apply vibrothermography to compare the sensitivity of their heating behaviour (global and local) with the crack density. A correlation between the heating and the loss of a mechanical property of the material (in this case the Young modulus) estimated with the tensile loading tests is also highlighted.

Nomenclature

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\varepsilon)</td>
<td>Sample thickness</td>
<td>mm</td>
</tr>
<tr>
<td>(E_T)</td>
<td>Tangential Young modulus</td>
<td>GPa</td>
</tr>
<tr>
<td>(L)</td>
<td>Sample length</td>
<td>mm</td>
</tr>
<tr>
<td>(\Delta T_{bulk})</td>
<td>Bulk heating rate</td>
<td>mK/s</td>
</tr>
<tr>
<td>(\Delta T_{surf})</td>
<td>Surface heating rate</td>
<td>mK/s</td>
</tr>
<tr>
<td>(\Delta T_{dam})</td>
<td>Damage heating rate</td>
<td>mK/s</td>
</tr>
<tr>
<td>(\Delta T_{visco})</td>
<td>Viscoelastic heating rate</td>
<td>mK/s</td>
</tr>
<tr>
<td>(\rho)</td>
<td>Density</td>
<td>Kg/m³</td>
</tr>
<tr>
<td>(C_T)</td>
<td>Specific heat</td>
<td>J/KgK</td>
</tr>
<tr>
<td>(\langle q_{dam}\rangle_T)</td>
<td>Equivalent damage volumetric source</td>
<td>W/m²</td>
</tr>
<tr>
<td>(\langle q_{visco}\rangle_T)</td>
<td>Equivalent viscoelastic volumetric source</td>
<td>W/m²</td>
</tr>
<tr>
<td>(\sigma)</td>
<td>Stress</td>
<td>MPa</td>
</tr>
</tbody>
</table>

1. Introduction

Woven composite materials, also known as textile composites, are receiving a growing interest in the industry applications thanks to their better mechanical performances in comparison with the traditional composite materials [1]. Their textile nature, characterised by the presence of the warp and the weft, guarantees a high flexibility of the reinforcement which permits the creation of very complex shaped structures [2, 3]. Unfortunately, this characteristic becomes a problem for the Non Destructive Evaluation (NDE) of this kind of material. The application of the standard NDE techniques, such as active thermography or US-scan is very complicated due to the inhomogeneities of this kind of material and to the non-uniform crack orientation [4, 5]. A solution to these problems can be searched in the vibrothermography technique. Vibrothermography, also named “Sonic IR” or “thermosonics” [6], is an NDE technique by which damage (cracks, delamination and inclusions) is detected using the heat locally generated by the friction between the defects surfaces when they are put in vibration. The first applications of this technique concern the detection of cracks in metals (in particular during fatigue tests) for which the technique has shown great potentialities [7, 8, 9, 10]. More recently, this technique has found applications to composite materials for the detection of macro-cracks, as delamination, or to evaluate the inhomogeneities in bonding joints [11, 12]. Other applications concern the study of corrosion [13] or the inspection of the welds between different materials [14].

As Renshaw et al. report [15], the heat generation is a consequence of three phenomena: friction between crack surfaces, viscoelasticity and plasticity. In particular, the first one is considered as the principal source of heat generation. Some models based on the crack nature (friction coefficient, roughness...) have been developed for the estimation of the heating generated [16], but the link with the crack geometry is still complicated [11]. The contribution of the viscoelastic properties can be negligible for metals, but it can be very important for polymeric materials (like the materials analysed in this paper) [17]. Finally, the heat generation caused by plasticity can be considered as a consequence of the friction or, to a lesser extent, of crack propagation [18]. This contribution can be negligible if the excitation stress is less than 40% of the fatigue limit of the material [8]. Some models can estimate this vibrational stress knowing the mechanical properties of the material [19, 20, 21].

Most of these works here mentioned aim at detecting macro-cracks (with a characteristic length of some centimetres) which is not the goal of this paper. This study focuses on the application of vibrothermography to a micro-cracking damaged material (characteristic length of some micrometers). The goal is not the direct detection of each single crack, but to find a technique that is sensitive to a damage which is supposed to be homogeneously diffuse in terms of crack density. After the presentation of the experimental set-up, the results of the tests phase are reported. First, the results of the tensile loading tests are discussed followed by the results of the vibrothermography tests. Some conclusions and observations are reported in the final part of this paper.
2. Experimental approach

The studied material is a 4 plies, 1.6 mm thick glass/epoxy 2D woven composite. Three samples of this material (25 x 185 mm) are damaged by tensile tests stopped at different loads, in order to obtain different damage states. The tensile testing machine is monitored with image correlation cameras, optical microscope and acoustic emission sensors in order to collect different data from the tests and define each damage level of the material. In particular, the first sample is monitored with the acoustic emission, up to its failure (280 MPa). The cumulative acoustic energy is then used to select the other two damage levels: one is a close-to-failure damage level at 250 MPa, and the other one is a low damage level at 190 MPa. The microscope acquires images of the cross-section in order to estimate the damage state of each sample in terms of a crack density. The image correlation cameras along with the machine force signal permit to extrapolate the stress-strain variation of the material that can be used to calculate the variation of the Young modulus during the tests. All these quantities can be correlated between each other in order to estimate how the damage state of the material could influence the mechanical properties of the material, as reported in the results section of this paper.

In a second phase, vibrothermography tests are performed to study the influence of the damage on the thermal behaviour of the material when it is excited at a fixed frequency. The vibrothermography testing set-up, as illustrated in figure 1 is composed of a fixed structure where the sample can be positioned to obtain different fixation conditions. A symmetric configuration is recommended in order to be sensitive only to the damage state of the material. To optimise the vibration behaviour of the material, a fixed-fixed condition is chosen in this study. The samples are excited by a piezoelectric vibration generator (Meggitt Wilcoxon Research model F7) with a usable frequency range of 500-20,000 Hz. Different excitation frequencies are studied, but only the results for a frequency of 5 kHz are reported here. This frequency is close to a resonant frequency of the samples that can guarantee the best results in terms of temperature variation as reported in [22, 23, 24]. Thermal images are acquired by an infrared camera (FLIR X6540) during 180 seconds at a 50 Hz frequency with an integration time of 3000 μs (to obtain the necessary resolution of above some tenths of a degree) [25].

![Fig. 1. Experimental setup for vibrothermography.](image-url)

To insure the best reproducibility of the vibrothermography tests, different parameters that can influence the tests are taken into account. As reported in [26, 27], the most important factors are the coupling between the exciter and the sample, and the sample fixation conditions. As mentioned in [28, 29], a coupling material can be essential to obtain better results. In fact, a permanent contact with the shaker avoids all the phenomena connected to the non-linearities of the coupling. During this work, a double-sided bonding tape is used to introduce the perfect coupling between the exciter head and the sample surface that can guarantee the reproducibility of the tests. The same tightening fixation torque at both of the extremities of the samples also permits a symmetrical initial condition of the sample. Every possible initial thermal gradient that could be noticed between the samples and the fixation structure will not influence the final results because only temperature variations are studied (and so all the initials inhomogeneities are eliminated by subtraction).
3. Results

The first part of this section is dedicated to the results of the tensile loading tests. For each sample, an observation of micro-cracking by microscope is performed to evaluate an equivalent crack length and a crack density to characterise the damage level. The tangential elastic modulus variation is then estimated and correlated with the crack density of the samples. The second part concerns the analysis of the vibrothermography tests. A comparison between damaged and undamaged states of the material is reported to study the influence of cracks in the thermal behaviour of the material; in particular, a global and a local analysis are performed. A correlation between the damaged conditions and the heating velocities of the samples is reported.

3.1. Tensile tests results

![Image of tensile test results]

**Fig. 2.** Left: cross-section microscopy picture of the sample damaged at 250 MPa. Right: Visual comparison between undamaged sample and damaged (250 MPa) sample surfaces.

The first result reported here is a study of the typology of the damage generated during the tensile loading tests. Figure 2 (left) shows a zoomed area of a cross-section microscope picture for a sample damaged at 250 MPa on which it is possible to identify each kind of damage. Basically, two different families of crack can be defined: fibres ruptures, with a characteristic dimension of 25 µm, diffuse and homogeneous in all the material, and intra/inter-yarn decohesions that have a medium dimension of 250 µm and that are present locally. Figure 2 (right) also shows two images that make able to evaluate by naked eye the presence of the multiple cracking in the material in comparison with an undamaged sample. It can be noted that the damage is present along the entire width of the sample and not concentrated only at its edges. This consideration enables to make the hypothesis that the damage observed by microscopy on the cross-section is representative of the global damage condition of the sample. This hypothesis supports the introduction of a parameter that can indicate the damage level of each sample, named crack density (β) that is defined in Eq. (1)

$$ \beta = \frac{\int_0^L t_c^{eq} \, dx}{eL} $$

(1)

where e is the thickness of the sample, L its length and $t_c^{eq}$ (equivalent crack length) is the sum of the lengths of each crack detected by microscopy as reported in figure 3.

![Image of equivalent crack length estimation]

**Fig. 3.** Estimation of the equivalent crack length $t_c^{eq}$ for the damaged samples along the length of samples in the accessible field acquired by microscopic observation.
The spatial repartition of $t_{IC}$ along the samples damaged at 190 MPa and 250 MPa is reported in figure 3. It is important to notice that the sample loaded at 190 MPa is homogeneously damaged; unlike the second sample that presents a slight asymmetry. For each sample, the estimated average $t_{IC}$ is indicated. The value of the crack density estimated for each sample is reported in table 1. It is checked that the sample damaged at 250 MPa has a doubled crack density compared to the sample loaded at 190 MPa.

<table>
<thead>
<tr>
<th>Sample load [MPa]</th>
<th>Crack density [mm$^{-1}$]</th>
</tr>
</thead>
<tbody>
<tr>
<td>190</td>
<td>0.34</td>
</tr>
<tr>
<td>250</td>
<td>0.69</td>
</tr>
</tbody>
</table>

The data of the image correlation cameras enable to determine the stress-strain curves for each sample and to compare them as reported in figure 4.

As observed in figure 4, the three curves have a similar behaviour which demonstrates that the considered samples are representative of the material. For each sample, it is possible to estimate the tangential Young modulus $E_T$ at the beginning and at the end of the tensile test (figure 5) in order to calculate its variation. This parameter can be compared with the crack density of the sample, as reported in figure 6, in which a linear trend of these two parameters is observed.

![Fig. 4. Stress-strain curves for the three samples.](image)

![Fig. 5. Estimation of the Young modulus variation.](image)

![Fig. 6. Correlation between the crack density ($\beta$) and the Young modulus variation.](image)
3.2. Vibrothermography results

In this section, the results of the vibrothermography tests are reported. The first analysis that can be conducted is to observe the thermal behaviour of the surface of the sample as function of the damage level. Two parameters can be studied: the average heating of the surface (figure 7) and the standard deviation of the measures (figure 8). In particular, figure 7 shows that the average heating of the samples depends on the damage level of the material: the more damaged the sample is, the higher the final heating is. A second observation concerns the behaviour of the undamaged sample that presents a temperature variation during the excitation. This heating cannot be created by friction of cracks in the material (it is undamaged), but it is a consequence of the viscoelastic nature of the material, as also observed in [30].

These results demonstrate that the contributions to the heating are cracks frictions and viscoelasticity. A simple thermal model can be introduced to correlate these quantities with the heating rate of the sample, as reported in Eq. (2),

\[ \rho C_p \Delta T_{\text{bulk}} = \rho C_p \Delta T_{\text{surf}} = (q_{\text{dam}})T + (q_{\text{visco}})T \]  

(2)

where \( (q_{\text{dam}})T \) and \( (q_{\text{visco}})T \) are the equivalent constant volumic heat sources (averaged over a period of the excitation frequency) generated by damage and viscoelasticity, respectively; \( \rho \) is the material density and \( C_p \) is the specific heat. With the hypothesis that the heat transfers by conduction and convection are neglected, the equivalence between surface heating rate \( \Delta T_{\text{surf}} \) and bulk heating rate \( \Delta T_{\text{bulk}} \) can be assumed. The quasi-linearity of the heating observed in figure 7 indicates that the sources terms introduced in the model (Eq. 2) may be considered as constants during the excitation time. This makes it possible to introduce two new parameters named damage heating rate \( \Delta T_{\text{dam}} \) and viscoelastic heating rate \( \Delta T_{\text{visco}} \) as defined in Eq. (3)

\[ \Delta T_{\text{surf}} = \frac{(q_{\text{dam}})T}{\rho C_p} + \frac{(q_{\text{visco}})T}{\rho C_p} = \Delta T_{\text{dam}} + \Delta T_{\text{visco}} \]  

(3)

With the hypothesis that the viscoelastic heating rate \( \Delta T_{\text{visco}} \) is the same for all the samples (it is independent of the damage level of the material), the contribution of damage to the heating rate of the sample \( \Delta T_{\text{dam}} \) can be estimated by subtraction from experiments on the undamaged sample. The values computed from linear regression for each sample are indicated in table 2.

Table 2. Heating rates estimated: global and damage heating

<table>
<thead>
<tr>
<th>Sample load [MPa]</th>
<th>( \Delta T_{\text{surf}} ) [mK/s]</th>
<th>( \Delta T_{\text{dam}} ) [mK/s]</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>190</td>
<td>1.3</td>
<td>0.6</td>
</tr>
<tr>
<td>250</td>
<td>1.9</td>
<td>1.2</td>
</tr>
</tbody>
</table>

Figure 8 shows the time evolution of the standard deviation for the three samples. The growth of the standard deviation indicates that the heating of the material is not spatially homogeneous, so the source terms in Eq. (2) are dependent on space coordinates (by definition, a uniform heating would not influence the standard deviation). Then, the absence of the spurious heating peaks that it is possible to observe in the average heating of figure 7 (for example between 90 s and 100 s for the undamaged sample) indicates that these discontinuities are a global phenomenon that influences the entire sample and are a consequence of some external perturbations. Finally, the initial standard deviation (at t = 0 s) is an indicator of the thermal noise level (at the initial time, the vibrothermographic effect due to the friction between cracks is null), and is similar for each test.
The thermal images, as those reported in figure 9, qualitatively show the heating behaviour of the sample damaged at 250 MPa. In the image are present the alternated zones with localised heating anticipated by the analysis of the standard deviation. To understand the nature of the formation of these zones, figure 10 shows a correlation between the heating of the sample and the squared out-of-plane velocity amplitude acquired thanks to a Laser vibrometer. The spatial correlation observed between normalised heating and normalised vibration velocity suggests that the heating is maximal at the maximum vibration of the sample, in agreement with previous results from the literature [30]. The maximum heating is in correspondence with the exciter position in the middle of the sample (as shown in figure 9). Heating and velocity in this region are imposed by the exciter dynamics. The asymmetrical heating that can be identified on figure 9 can be explained by the fact that the sample presents a damage condition that it is not homogeneous in the material, as demonstrated by the equivalent crack length \( l_c^{eq} \) in figure 3. In particular, the most damaged part of the sample generates a higher heating level.

**Fig. 8.** Standard deviation for the three samples.

**Fig. 9.** Thermal image (heating) of the sample damaged at 250 MPa (black & white and colours).

**Fig. 10.** Spatial correlation between the normalised heating (red) and the normalised vibrational velocity (blue).
A local study of the heating of these zones can be achieved by looking at the temperature variations for each zone as reported in figure 11. In particular, an alternation of zones with high heating (odd numbered) with zones of lower heating (even numbered) can be observed. The zones with lower heating have a very similar behaviour; however, for the other zones the heating depends on the position of the excitation point (the closer the zone is to the centre of the sample the higher the total heating is). An explanation for this phenomenon is yet under study.

Fig. 11. Thermograms of the localised zones

A correlation between the damage heating rate $\Delta T_{dam}$ and the damaged conditions of the sample (characterised by the crack density $\beta$) and the loss of a mechanical property are reported, respectively, in figure 12.a and 12.b. A linear correlation trend between these parameters can be observed and the two corresponding coefficients that can characterise the material studied in this work can be estimated.

Fig. 12. A) Correlation between vibrothermographic heating velocity and: the crack density $\beta$ (A) and the Young modulus variation (B)
4. Conclusions

Table 3. Samples results

<table>
<thead>
<tr>
<th>Parameter</th>
<th>190 MPa</th>
<th>250 MPa</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \sigma )</td>
<td>190 MPa</td>
<td>250 MPa</td>
</tr>
<tr>
<td>( \varepsilon )</td>
<td>1.08%</td>
<td>1.47%</td>
</tr>
<tr>
<td>( \Delta E_T )</td>
<td>6.2%</td>
<td>11.8%</td>
</tr>
<tr>
<td>( \beta )</td>
<td>0.34 mm/(^1)</td>
<td>0.69 mm/(^1)</td>
</tr>
<tr>
<td>( \Delta T_{\text{dam}} )</td>
<td>0.6 mK/s</td>
<td>1.2 mK/s</td>
</tr>
<tr>
<td>Standard deviation</td>
<td>0.06 K</td>
<td>0.08 K</td>
</tr>
</tbody>
</table>

In table 3 are reported the most important results of this study in order to compare the different parameters. In conclusion this work has demonstrated that:

- The studied material presents a growing damage level with the loading condition that it is quantifiable by a crack density parameter.
- The global heating of the sample is a function of the damage level of the material.
- The contribution due to the viscoelastic properties of the material is identified and quantified using the undamaged sample.
- The study of the standard deviation put in evidence that the heating of the material is not uniform; there is the formation of some alternated zones visible by the thermal images. The local heating of the material is a function of the vibrational mode of the sample.
- The global heating rate of the material can be correlated with the loss of a mechanical property and the damage levels of the material. A linear correlation trend was observed in this study.

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