

## Discrete Trigonometric Transform Thermography for Defect Detection in Composites

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### Abstract

Images obtained with Pulsed Thermography (PT) are often affected by noise and non-uniform heating. Therefore, numerous advanced signal processing methods have been proposed to solve these problems and thus improve the defects detection that are below the surface of materials. Some of these techniques are Principal Component Thermography (PCT), High-Order Statistics (HOS), Thermographic Signal Reconstruction (TSR) –and its first and second derivatives–. However, none of these methods is based on the law of conservation of energy of a signal (i.e., each image or thermogram) between space and frequency domains. With this approach we developed an algorithm to detect defects in Carbon Fiber Reinforced Plastic (CFRP) composites. To do this we evaluated four types of Discrete Cosine Transforms (DCTs): DCT-1, DCT-2, DCT-3, DCT-4; and four types of Discrete Sine Transforms (DSTs): DST-1, DST-2, DST-3, DST-4. Comparison between results of the Contrast-to-Noise Ratio (CNR) metric shows that if the proposed algorithm uses DCT-1, then it outperforms second derivative of the TSR. Furthermore, this method is robust against changes in shape or non-uniform heating center. To our knowledge, the potential of these transforms for use in pulsed thermography has never before been evaluated.

### 1. Introduction

The DCTs/DSTs began to be discovered by the electronic engineer Nasir Ahmed in 1974. In total there are sixteen transforms, eight DCT and eight DST. The most recognized and used in the world is the DCT-2 for its insurmountable property of compacting the energy of the images in the spatial domain, in very few coefficients in the frequency domain. Two of the direct two-dimensional definitions of the DCTs/DSTs tested are presented in Eqs. (1) and (2).

$$DCT - 1: \quad X^{c1}(k_1, k_2) = p(k_1)p(k_2) \sum_{n_1=0}^{N_1-1} \sum_{n_2=0}^{N_2-1} q(n_1)q(n_2)x(n_1, n_2) \cos\left(\frac{2\pi}{2(N_1-1)}n_1k_1\right) \cos\left(\frac{2\pi}{2(N_2-1)}n_2k_2\right) \quad (1)$$

$$DCT - 2: \quad X^{c2}(k_1, k_2) = p(k_1)p(k_2) \sum_{n_1=0}^{N_1-1} \sum_{n_2=0}^{N_2-1} x(n_1, n_2) \cos\left(\frac{\pi}{2N_1}(2n_1+1)k_1\right) \cos\left(\frac{\pi}{2N_2}(2n_2+1)k_2\right) \quad (2)$$

where,

- $x(n_1, n_2)$  is each image coming from the thermal camera (i.e., the thermograms).
- $N_1, N_2$  are the numbers of pixel rows and pixel columns in each thermogram.
- $n_1, n_2$  are the pixel indices (in the spatial domain) of the thermogram  $x(n_1, n_2)$ .
- $k_1, k_2$  are the coefficient indices (in the frequency domain) of the transformed thermogram  $X(k_1, k_2)$ .
- $X^{c1}(k_1, k_2)$  is the transformed thermogram obtained by applying DCT-1 to  $x(n_1, n_2)$ .
- $X^{c2}(k_1, k_2)$  is the transformed thermogram obtained by applying DCT-2 to  $x(n_1, n_2)$ .
- $p(k_1), p(k_2), q(n_1), q(n_2)$  are weighting functions to ensure energy conservation between the spatial domain and the frequency domain.

To calculate the DCT/DST to a thermogram ( $N_1 \times N_2$  matrix), simply calculate the one-dimensional transform to each row and each column of that thermogram. This can be done since the DCTs/DSTs have separable basis functions.

### 2. Materials and Methods

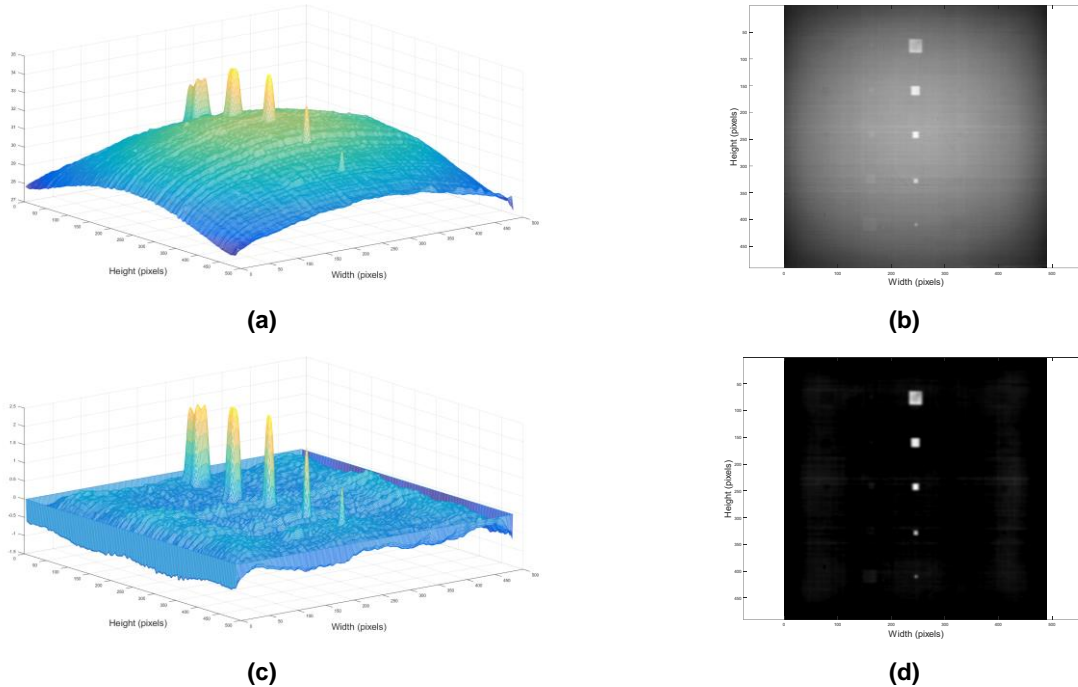
As materials, Infrared image sequences obtained with an experimental set-up consisting of a FLIR X8501sc camera, electric charge and synchronization units, and two Balcar FX60 flashes were used. The tested specimen was a flat CFRP sheet with 25 Teflon inlays inside to mimic defects. The defects are found at depths of 0.2 mm, 0.4 mm, 0.6 mm, 0.8 mm and 1.0 mm; and have sizes from 3 x 3 mm<sup>2</sup> to 15 x 15 mm<sup>2</sup>.

Regarding the methods, the main procedure of this algorithm consists of taking each thermogram of the infrared image sequence and transforming it with each of the DCTs/DSTs. Then, in the frequency domain, those coefficients that store the energy associated with non-uniform heating are eliminated. Such coefficients are very few and are located in the upper left corner of the transformed thermogram. Subsequently, the thermogram is returned to the spatial domain with the corresponding inverse transform.



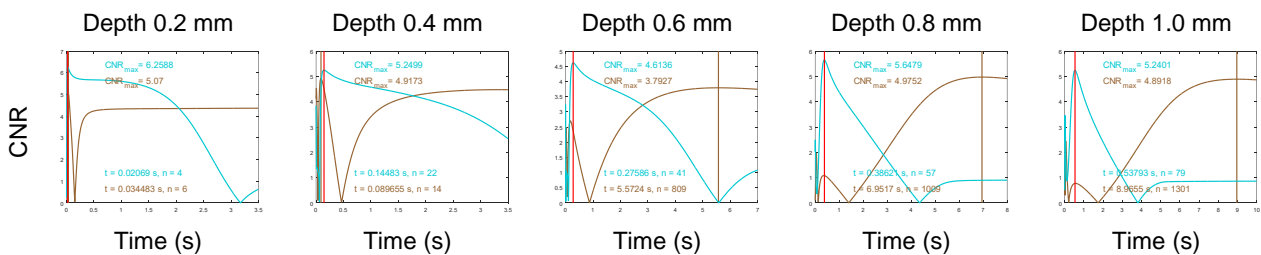
### 3. Results and Conclusion

The most remarkable result is elimination of non-uniform heating regardless of its shape or the location of its middle, which is very convenient in case there are changes in orientation of the heat sources (i.e. the flashes). Figure 1 shows as an example the thermogram 13 –from infrared inspection of CFRP– before and after processing it with DCT-1.

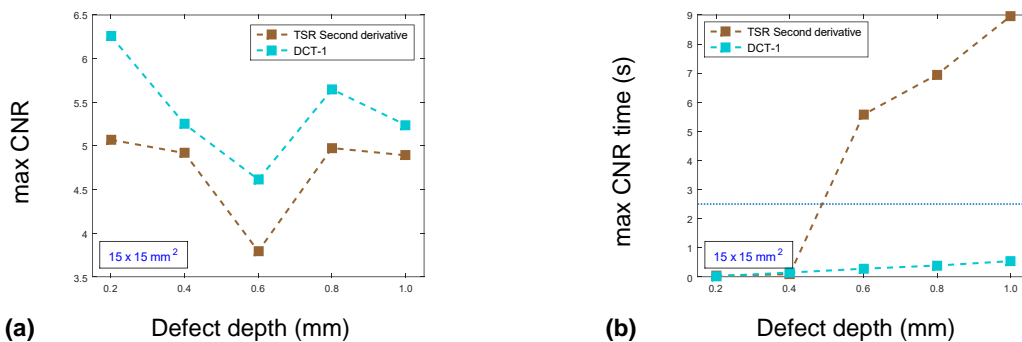


**Fig. 1.** Thermogram 13 of the infrared inspection. The central column of defects located at a 0.2 mm depth in the CFRP plate is observed. (a) and (b) before processing it with DCT-1. (c) and (d) after processing it with DCT-1.

Figure 2 shows CNR plots of the five largest defects, size 15 x 15 mm<sup>2</sup>. The CNR was measured for each defect in all thermograms, which were processed with the proposed method based on DCT-1 and compared with the second derivative of the TSR. Figure 3(a) shows that in all measures of maximum CNR, DCT-1 outperforms TSR 2nd derivative.



**Fig. 2.** CNR for second derivative of the TSR (brown plots) and DCT-1 (aquamarine plots). All plots for the same infrared inspection. Size of defects: 15 x 15 mm<sup>2</sup>



**Fig. 3.** Comparisons between second derivative of the TSR and DCT-1. Size of defects: 15 x 15 mm<sup>2</sup>. (a) maximum CNR as a function of the defect depth. (b) maximum CNR time as a function of the defect depth.